An Intelligent Method Based on State Space Search for Automatic Test Case Generation

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Abstract—Search-Based Software Testing reformulates testing as search problems so that test case generation can be automated by some chosen search algorithms. This paper reformulates path-oriented test case generation as a state space search problem and proposes an intelligent method Best-First-Search Branch & Bound to solve it, utilizing the algorithms of Branch & Bound and Backtrack to search the space of potential test cases and adopting bisection to lower the bounds of the search space. We also propose an optimization method by removing irrelevant variables. Experiments show that the proposed search method generates test cases with promising performance and outperforms some MetaHeuristic Search algorithms.

Index Terms—Search-Based Software Testing, test case generation, Branch & Bound, backtrack, state space search, bisection

I. INTRODUCTION

Software is being integrated into more and more systems, so it is becoming increasingly important to fully test these systems. One challenge to testing software systems is how to generate test cases systematically in an effective fashion [1]. It is estimated that testing cost has accounted for almost 50 percent of the entire development cost [2], if not more. Therefore, a rational response is to automate the testing process as much as possible, and automatic test case generation naturally plays a key role in this process [3]. Specifically, the automation of path-oriented test case generation (which belongs to the typical control flow testing including those using statement coverage, branch coverage and MC/DC coverage) will efficiently improve testing quality and save the cost of software development [4].

A trend in the automation of path-oriented test case generation is the application of MetaHeuristic Search (MHS) algorithms [5]. The main reason is that test case generation problems can often be reexpressed as search problems. Some MHS algorithms that have been employed for Search-Based Software Testing (SBST) are genetic algorithms [6], simulated annealing [7], and ant colony optimization [8]. These algorithms all require the actual execution of the Program Under Test (PUT) and the results are not definite. That is, due to the adoption of the theory of probability they are categorized as cut-and-try methods. Usually a large amount of iterations are made to automatically generate an input which meets the coverage criteria, sometimes causing iteration exception. Therefore, choosing the right algorithm for the problem is very crucial to the search [9].

In this paper, considering the drawbacks of MHS methods mentioned above and on the base of static analysis techniques including interval computation, we introduce the algorithms of Branch & Bound and Backtrack from the field of artificial intelligence to tackle the problem of path-oriented test case generation, which is reformulated as state space search. Bisection is used to lower the bounds of the search space. We also make optimization by irrelevant variable removal (IVR). We have made experiments on C programs, and the results show that the proposed method performs encouragingly in test case generation and has an advantage over some MHS methods in terms of coverage.

The rest of this paper is organized as follows: Section II introduces some relevant concepts including Branch & Bound, Backtrack and bisection; Section III reformulates path-oriented test case generation as a state space search problem; Section IV overviews how the state space is searched dynamically; Section V describes the proposed algorithm and its details; Section VI implements experiments and presents analysis to the results; Section VII concludes this paper and provides the direction of future work.

II. RELATED WORK

Branch & Bound (BB) [11] is an efficient method for searching the solution space of a problem. The advantage of the BB strategy lies in alternating branching and bounding operations on the set of active and extensive nodes of a search tree. Branching refers to partitioning of
the solution space (generating the child nodes); bounding refers to lowering bounds used to construct a proof of feasibility without exhaustive search (evaluating the cost of new child nodes). In BB frame, bisection [12] is often used to help prune unneeded part of the solution space. Bisection is also normally used in test case generation [13].

Backtrack [14] is an optimum seeking method which searches forward according to the selection conditions to achieve a goal. If at a certain step of the search, it is found that the goal turns out to be unachievable, then a step backward is taken. The point satisfying the backtrack condition is a backtrack point.

In classical BB search, nodes are always fully expanded, that is, for a given leaf node, all child nodes are immediately added to the so called open list. However, considering that only one solution is enough for path-oriented test case generation, Best-First-Search is our first choice, so permutation of variables is required for branching to prune the branches stretching out from unneeded variables. Meanwhile because the domain of a variable is a finite set of possible values which may be quite large, bounding is necessary to cut the unneeded or infeasible solutions. Hence this paper proposes a new algorithm Best-First-Search Branch & Bound (BFS-BB) that conducts state space search dynamically to find the test case. We also integrate Backtrack algorithm to make full use of the past data obtained during the search process.

III. REFORMULATION OF THE PROBLEM

Many forms of test case generation make reference to the control flow graph (CFG) [15] of the program in question. A CFG for a program \( P \) is a directed graph \( G=(N, E, s, e) \), where \( N \) is a set of nodes, \( E \) is a set of edges, and \( s \) and \( e \) are respective unique entry and exit nodes to the graph. Each node \( n \in N \) is a statement in the program, with each edge \( e=(n,n_i) \in E \) representing a transfer of control from node \( n \) to node \( n_i \). A path \( p \) through a CFG is a sequence \( p=(n_i,n_2,...,n_n) \), such that for all \( r, 1 \leq r < g, (n_i,n_{r+1}) \in E \). A path is said to be feasible if there exists a program input for which the path is traversed, otherwise the path is said to be infeasible. The feasibility of a path is judged by interval computation. Interval computation analyzes and calculates the ranges of the variables’ values in the PUT and provides precise information for further program analysis [16]. We enhance interval computation by adding a library of inverse functions in case of the occurrences of library functions in the PUT.

The path-oriented test case generation problem can be reformulated as a search problem: \( X \) is a set of variables \( \{x_1,x_2,...,x_n\} \), \( D=\{D_1,D_2,...,D_n\} \) is the set of domains and \( D_i \subseteq D_i \) is a finite set of possible values for variable \( x_i \). For each path, \( D \) is defined based on the variables’ acceptable ranges. One solution to the problem is a set of values for each variable inside its domain denoted as \( V=\{V_1,V_2,...,V_n\} \), \( V_i \subseteq D_i \), to make the path feasible. There might be one, more or no solutions. If there is at least one solution, then the search succeeds otherwise it fails. The solution space is represented by a dynamically constructed tree where each node represents a step of the search. With the aid of intelligent rules for selecting nodes to explore and pruning those that do not lead to a solution, the complexity of the search can be drastically reduced as compared to that of an exhaustive implicit enumerative search. The search process is based on the result of interval computation and a heuristic estimate of the remaining part.

IV. OVERVIEW OF BFS-BB

We introduce state space search [17], which is an important issue in artificial intelligence to tackle the search problem. In order to facilitate the implementation of BFS-BB, we propose the following definitions.

Definition 1. A state space is a quadruple \( (S, A, I, F) \), where \( S \) is the set of states, \( A \) is the set of arcs or connections between the states including Permutate, Select, Reduce Domain and Backtrack that correspond to the steps or operations of the search at different states, \( I \) is a non-empty subset of \( S \) denoting the initial state of the problem and \( F \) is a non-empty subset of \( S \) denoting the final state of the problem.

Definition 2. A state is a tuple \( \langle \text{Precursor}, \text{Variable}, \text{Domain}, \text{Value}, \text{Type}, \text{Queue} \rangle \). In a certain stage of the search process, from the perspective of current state \( S_{cur} \), Precursor provides a link to the previous state; \( \text{Variable}=x_i \in X \ (i=1,2,...,n) \) is an input variable of PUT; \( \text{Domain}=D_j \subseteq D_j \ (i=1,2,...,n; \ j=1,2,...,m) \) in the form of \([\min, \max]\) is the current domain of \( \text{Variable} \) which is the set of possible values that may be selected for \( \text{Variable} \); \( \text{Value}=V_j \subseteq D_j \) is a value selected from \( \text{Domain} \); Type marks the type of \( S_{cur} \) which may be active, extensive or inactive; \( \text{Queue} \) is a sequence of variables corresponding to \( S_{cur} \).

Definition 3. State space search is all about finding, in a state space (which may be extremely large), one final state. Final means that every variable has been given a definite value successfully and the path is proved to be feasible with all these values by interval computation. At the start of the search \text{Precursor} is null, and when \text{Queue} is null the search ends. The path made up of all the extensive states makes the solution path of the search. State space search is accomplished by BFS-BB in this paper.

When constructing each state, Type is active. \text{Queue} is the head of \text{Queue}. An interval computation is carried out to each active state to determine the direction of the next step of search. If the interval computation succeeds, then Type becomes extensive, the remaining variables will be permuted to get \text{Queue} and \text{Variable} becomes \text{Precursor}, and the head of \text{Queue} will be \text{Variable} of next state. If interval computation fails, Type remains active, according to the information from the failed interval computation \text{Reduce domain} is conducted with bisection, and \text{Value} is reselected from the reduced domain, all of which mean the search will expand to a state with a different value for the same variable. If for the same variable all the values within its domain are tried out or the interval computation
for it has reached the time limit $m$ (which is the branching factor, or a threshold used to control the breadth of the search tree, namely, the limit on the number of times of interval computation taken for one variable under the same condition), then its Type becomes inactive, indicating that the search arrives at a backtrack point and will have to backtrack to the previous state Precursor at the higher level of the search tree.

The process of generating a test case for path $p$ takes the form of state space search. We need to search the state space to find a solution path from an initial state to a final state. We can decide where to go by considering the possible moves from the current state, and trying to look ahead as far as possible.

V. DETAILS OF BFS-BB

We proceed by first giving an outline of algorithm BFS-BB and then giving the detailed explanations to the key parts. The outline of BFS-BB is shown in Fig.1.

Figure 1. The outline of the search algorithm
A. Irrelevant Variable Removal

As mentioned above, \(X=\{x_1, x_2, \ldots, x_n\}\) is the set of input variables for the program \(P\). The state space should concern every \(x_i\) \((i=1, 2, \ldots, n)\) in \(X\). However, it is possible that not every input variable will be responsible for determining whether every path in \(P\) will be traversed or not. A simple example follows with a program \(test_1\) and its corresponding CFG shown in Fig. 2 where \(if\_out_5, if\_out_6\) and \(exit_7\) are virtual nodes. Adopting branch coverage, there are three paths to be covered, while the input variable \(x_3\) is only relevant to Path 2: \(0->1->3->4->5->6->7\) and Path 3: \(0->1->3->5->6->7\), but not to Path 1: \(0->1->2->6->7\). The numbers along the path denote nodes rather than edges of the CFG. Therefore, when attempting to generate test case for Path 1, search effort on the value of \(x_3\) is wasted since it cannot influence the traversal of Path 1. Thus, removing irrelevant input variables from the search space and only concentrating on input variables relevant to the path of interest may improve the performance of the search process. Relevant and irrelevant variables are defined as follows.

**Definition 4.** A relevant variable is an input variable that can affect whether a particular path \(p\) will be traversed or not. To put it more precisely, for all the input variables \(\{x_i\} | x_i \in X, i=1, 2, \ldots, n\), there exists a corresponding set of values \(\{V_i\} | V_i \in D_i, i=1, 2, \ldots, n\), with which \(p\) is not traversed, but when the value of a particular variable is changed, for example, when the value of \(x_i(V_i)\) is changed into \(v_i\), \(p\) is traversed with the input \(\{x_1, x_2, \ldots, x_i, v_i \ldots, x_n\}\), then \(x_i\) is a relevant variable to path \(p\).

**Definition 5.** An irrelevant variable is an input variable that is not capable of influencing whether a particular path \(p\) will be traversed or not. To put it more precisely, for all the sets \(\{V_i\} | V_i \in D_i, i=1, 2, \ldots, n\) of the search space of path \(p\), with which \(p\) is not traversed, regardless of the value in the change of a particular variable, for example, the value of \(x_i(V_i)\) is changed into \(v_i\), \(p\) is still not traversed with the input \(\{x_1, x_2, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n\}\), then \(x_i\) is an irrelevant variable to path \(p\)

Generally, for a particular path, whether an input variable is relevant or irrelevant cannot be completely determined due to the complex structure of programs [18]. But we can make conservative estimate of irrelevancy with static analysis techniques. Irrelevant variable removal (IVR) can result in test case being searched out with fewer interval computations for a particular path \(p\) than if all variables are considered.

B. Reducing Domain

Bisection is used to reduce the domain of a variable which has been selected a value making path \(p\) infeasible, together with Tendency, which is a property of a variable at a certain position (especially at branches of a CFG) providing the direction of the next step of search.

**Definition 6.** Tendency map is a mapping table \(<Variable, Tendency>\) denoting the relationship between Variable and Tendency held by a specific branch \(Br\) along path \(p\). Tendency is determined by branch predicates and expressions at the branch.

Note that there might be more than one tendency maps in a program, for each of them is held by a single branch. Still take \(test_1\) as an example, as mentioned above there are three paths to be covered, which are Path 1: \(0->1->2->6->7\), Path 2: \(0->1->3->4->5->6->7\) and Path 3: \(0->1->3->5->6->7\), respectively. Accordingly we can get tendency maps as shown in Table 1.

Take Path 1 as an instance, if \(S_{out} = \{Pre,x_1,D_{ij},V_{ij},active,Q_{pre}\}\) and interval computation fails at branch \(T_1\), then we retrieve the corresponding tendency map and get the tendency of \(x_1\) as the result which is positive. Through the retrieval of tendency map we can propagate the constraints made up of the branch predicates in a more and more precise manner as presented by Fig. 3.

```
void test1(int x1, int x2, int x3)
{
    if (x1-x2>=0)
    {
        printf("Path 1\n");
        break;
    }
    else if (x3-x1>0)
    {
        printf("Path 2\n");
    }
    else
    {
        printf("Path 3\n");
    }
}
```

Figure 2. Program test1 and its corresponding CFG

<table>
<thead>
<tr>
<th>Path</th>
<th>Branch</th>
<th>Tendency map</th>
</tr>
</thead>
<tbody>
<tr>
<td>Path 1</td>
<td>T 1</td>
<td>(&lt;x_1, positive&gt;, &lt;x_2, negative&gt;)</td>
</tr>
<tr>
<td>Path 2</td>
<td>T 2</td>
<td>(&lt;x_1, negative&gt;, &lt;x_2, positive&gt;)</td>
</tr>
<tr>
<td>Path 3</td>
<td>T 3</td>
<td>(&lt;x_3, positive&gt;, &lt;x_1, negative&gt;)</td>
</tr>
<tr>
<td>Path 3</td>
<td>T 4</td>
<td>(&lt;x_3, negative&gt;, &lt;x_2, positive&gt;)</td>
</tr>
<tr>
<td>Path 5</td>
<td>T 5</td>
<td>(&lt;x_3, negative&gt;, &lt;x_1, positive&gt;)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Algorithm. Reducing Domain</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input</strong> (D_i = [\text{min}, \text{max}]): the domain of (x_i)</td>
</tr>
<tr>
<td><strong>Output</strong> (D_i): the reduced domain of (x_i)</td>
</tr>
</tbody>
</table>
| \begin{itemize}
| 1: \(j++\); |
| 2: \(Br = \text{position of failure}\); |
| 3: \(Tendency = \text{get}(x_j)\); |
| 4: retrieve the tendency map held by \(Br\) |
| 5: if \((\text{Tendency} == \text{positive})\) |
| 6: \(D_i = [V_{ij}, \text{max}]\); |
| 7: else if \((\text{Tendency} == \text{negative})\) |
| 8: \(D_i = [\text{min}, V_{ij}]\); |
| 9: return \(D_i\); |
| \end{itemize} |

Figure 3. The algorithm Reducing Domain
VI. EXPERIMENTAL RESULTS AND DISCUSSION

To observe the effectiveness of BFS-BB, we carried out a large number of experiments in our team Code Testing System (CTS). Within the CTS framework, the PUT is automatically analyzed, its basic information is abstracted to form the Abstract Syntax Tree (AST) [19], and its CFG is generated. According to the specified coverage criteria, the paths to be covered are generated and provided for BFS-BB as input. After test cases have been generated by BFS-BB, test drive is generated to provide the environment to execute the test case. There are some auxiliary functions in CTS, including coverage observation, presentation of the covered code lines as well as the execution results, and the management of test cases for the convenience of regression testing. These functions of CTS provide comfortable experience for users such as the testing personnel.

The experiments were performed in the environment of MS Windows 7 with 32-bits and run on Pentium 4 with 2.8 GHz and 2 GB memory. The algorithms were implemented in Java and run on the platform of eclipse. Section A presents a performance evaluation about BFS-BB, Section B concerns whether BFS-BB outperforms other commonly used MHS algorithms in terms of coverage. Four programs served as our test beds including a benchmark program used in CTS and three others in test case generation, and the details of them are shown in TABLE II.

### TABLE II.

**BENCHMARK PROGRAMS USED FOR EXPERIMENTAL ANALYSIS**

<table>
<thead>
<tr>
<th>Program</th>
<th>LOC</th>
<th>Variables</th>
<th>Description</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>branch_bound</td>
<td>402</td>
<td>27</td>
<td>A benchmark used in CTS</td>
<td>by authors</td>
</tr>
<tr>
<td>isValidDate</td>
<td>59</td>
<td>16</td>
<td>To check whether a date is valid or not</td>
<td>referring to[8]</td>
</tr>
<tr>
<td>calDay</td>
<td>72</td>
<td>3</td>
<td>To calculate the day of the week</td>
<td>referring to[20]</td>
</tr>
<tr>
<td>cal</td>
<td>53</td>
<td>5</td>
<td>To calculate the number of days between the two</td>
<td>referring to[21]</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>given days in the same year</td>
<td></td>
</tr>
</tbody>
</table>

A. Performance Evaluation

To evaluate the performance of BFS-BB in test case generation, test cases were automatically generated to meet three different coverage criteria: statement, branch, and MC/DC. In this section, we utilized branch_bound.c, which is a relatively long program for unit testing with 402 lines and 27 input variables and complex structure trying to include more content that might appear in real-world PUTs. Since not all of the 27 variables are relevant for a specific path, comparison of search time is made to evaluate the effect of IVR.

Results of branch_bound.c using different coverage criteria are shown in TABLE III. The numbers of paths and average branches are different owing to different coverage criteria taken. BFS-BB generated test cases for all the feasible paths, trying to reach 100% coverage. IVR had no significant influence on the coverage, but it did on the search time. After the adoption of IVR, the search time was reduced greatly. Our following analyses all involve BFS-BB with IVR.

For branch_bound.c, BFS-BB was able to cover almost every branch, and generating test cases took a few seconds for all the feasible paths. The MC/DC coverage [22] (which is relatively strict and subsumes statement coverage and branch coverage) did not reach 100%, because we set time limit for the search time for each path as well as the threshold $m$ mentioned above for each variable. But we achieved tolerable coverage within tolerable time. There exists a trade-off between efficiency and success rate.

### TABLE III.

**EXPERIMENTAL RESULT USING THREE DIFFERENT COVERAGE CRITERIA WITH BFS-BB**

<table>
<thead>
<tr>
<th>Adequacy criterion</th>
<th>Paths</th>
<th>Average Branches</th>
<th>Average Coverage %</th>
<th>Search time reduced by IVR%</th>
</tr>
</thead>
<tbody>
<tr>
<td>statement</td>
<td>61</td>
<td>29</td>
<td>100</td>
<td>34</td>
</tr>
<tr>
<td>branch</td>
<td>119</td>
<td>43.33</td>
<td>100</td>
<td>37</td>
</tr>
<tr>
<td>MC/DC</td>
<td>125</td>
<td>43</td>
<td>94</td>
<td>42</td>
</tr>
</tbody>
</table>

B. Coverage Evaluation

This section presents results from a practical comparison of BFS-BB with GA and SA on three different benchmark programs using branch coverage as the adequacy criterion, which offers a favorable trade-off between costs and efficiency [23]. The result is shown in TABLE IV.

It can be seen that BFS-BB reached 100% branch coverage on all three test beds which are relatively simple programs for BFS-BB and outperformed the algorithms in comparison.

The better performance of BFS-BB results from two factors. One is that random testing [24] is a cheap and easy technique that can obtain reasonable coverage, simple yet effective in finding software fault, so for most of the cases, BFS-BB reached a relatively high coverage for the first round of search with a high speed. The second is that MHS crashed on several occasions due to the iteration exception, while the probability of aborting is quite low for BFS-BB because it has no demand for iteration.
TABLE IV.
COMPARISON WITH SA AND GA USING BRANCH COVERAGE

<table>
<thead>
<tr>
<th>Program</th>
<th>Paths</th>
<th>Branches</th>
<th>GA Average Coverage (%)</th>
<th>SA Average Coverage (%)</th>
<th>BFS-BB Average Coverage %</th>
</tr>
</thead>
<tbody>
<tr>
<td>isValidDate</td>
<td>5</td>
<td>16</td>
<td>99.95</td>
<td>98.21</td>
<td>100</td>
</tr>
<tr>
<td>calDay</td>
<td>20</td>
<td>11</td>
<td>96.31</td>
<td>99.97</td>
<td>100</td>
</tr>
<tr>
<td>cal</td>
<td>7</td>
<td>18</td>
<td>99.02</td>
<td>99.27</td>
<td>100</td>
</tr>
</tbody>
</table>

VII. CONCLUSION AND FUTURE WORK

This paper presents an intelligent search algorithm for path-oriented test case generation that utilizes the classical search algorithms of Branch & Bound and Backtrack. Experiments show that BFS-BB with IVR performs well on C programs. We also conducted empirical experiments to compare BFS-BB with some commonly used MHS methods, which produced encouraging results. This paper makes two major innovative improvements.

First, path-oriented test case generation is often solved by optimizing techniques, which may often suffer from the problem of local minimal or the initial starting point being too far from the solution. Our approach is flexible because backtracking is used to change direction of the search with efficiency. Second, bisection with tendency maps and IVR are used to optimize BFS-BB and accelerate the search process.

Our future research concerns not only how to generate test cases to reach high coverage but how coverage criteria, generation approach, and system structure jointly influence test effectiveness. The fault-finding capability of test cases and the effectiveness of the generation approach will be our focus for future work.

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